

IMPORTANT QUESTIONS

Q1. If $xy = 180$ and $\text{HCF}(xy) = 3$, find the $\text{LCM}(xy)$

$\text{HCF} \times \text{LCM} = \text{PRODUCT OF NUMBERS}$

$$\text{LCM} = \text{PRODUCT} / \text{HCF} = 180 / 3 = 60$$

Q2. Three bells ring at an interval of 4, 7 and 14 minutes. All three bell rang at 6 am. When will the three bells will ring together next?

$$4 = 2 \times 2; 7 = 1 \times 7; 14 = 2 \times 7$$

$$\text{LCM}(4, 7 \ \& \ 14) = 2 \times 2 \times 7 = 28$$

Hence, the bell will ring together again at 6.28am

IMPORTANT QUESTIONS

Q3. The HCF, of two numbers a and b, is 5 and their LCM is 200. Find the product ab?

HCF x LCM = PRODUCT OF NUMBERS

Product of Nos = $5 \times 200 = 1000$

Q4. Three bells red, green and yellow flash at intervals of 80, 90, 110 seconds. All three flash together at 8.00 am. When will these bulbs flash together again?

$80 = 2^4 \times 5$; $90 = 2 \times 3^2 \times 5$; $110 = 2 \times 5 \times 11$

$\text{LCM}(80,90,110) = 2^4 \times 3^2 \times 5 \times 11 = 7920$ seconds

$= 7920/60 = 132$ min = 2 hour 12 min

Three bulbs will flash together again at 10.12 am

Q5. PROVE THAT $\sqrt{5}$ IS IRRATIONAL

PROOF

1. Let us assume that $\sqrt{5}$ is rational
 2. Hence $\sqrt{5} = a/b$, where a & b ($b \neq 0$) are coprime numbers.
 3. Squaring on both sides, we get $5 = a^2 / b^2$
 $a^2 = 5 b^2$ (1)
- therefore, we can write $a = 5c$ for some integer c .
4. Substituting for a , we get $25c^2 = 5 b^2$, that is, $b^2 = 5 c^2$ (2)
 5. From equation (1) & (2), a & b have at least 5 as a common factor, by theorem 1.3
 6. This contradicts our assumption that $\sqrt{5}$ is a rational number
 7. Hence $\sqrt{5}$ is irrational

Q6. Write whether $(2\sqrt{45} + 3\sqrt{20}) / 2\sqrt{5}$ on simplification gives a rational number or an irrational number?

$$\begin{aligned}(2\sqrt{45} + 3\sqrt{20}) / 2\sqrt{5} &= (2 \times \sqrt{9 \times 5}) + \\ 3\sqrt{4 \times 5} / 2\sqrt{5} &= (2 \times 3\sqrt{5} + 3 \times 2 \times \sqrt{5}) / 2\sqrt{5} \\ &= (6\sqrt{5} + 6\sqrt{5}) / 2\sqrt{5} = 12\sqrt{5} / 2\sqrt{5} = 6, \text{ which is a} \\ &\text{rational number}\end{aligned}$$

Q7. Can two numbers have 16 as their HCF and 360 as their LCM?. Give reasons

No. Since HCF of two numbers, is a factor of their LCM. Here, HCF 16 is not a factor of LCM 360.

Q8. The decimal expression of $15/400$ will terminate after how many decimal places?.

$$\begin{aligned} 15/400 &= (3 \times 5) / (2^4 \times 5^2) = 3 \times 5 \times 5^2 / (2^4 \times 5^4) \\ &= 15 \times 25 / 10^4 = 375 / 10000 = 0.0375 \end{aligned}$$

Hence, it will terminate after 4 decimal places.

Q9. The decimal expression of $14587/1250$ will terminate after how many decimal places?.

$$\begin{aligned} 14587/1250 &= 14587 / (2 \times 5^4) \\ &= 14587 \times 2^3 / (2^4 \times 5^4) \\ &= 14587 \times 8 / (10^4) = 116696 / 10000 \end{aligned}$$

Hence, it will terminate after 4 decimal places.

Q10. If two positive integers a and b are written as $a = x^3 y^2$ and $b = x y^3$; x and y are prime numbers. Find $\text{LCM}(a, b)$?

$$a = x^3 y^2 \quad \text{and} \quad b = x y^3$$

LCM = greatest power of numbers

$$\text{LCM}(a, b) = x^3 y^3$$

Q11. what is the HCF of smallest composite number and the smallest prime number?

The smallest composite number = $4 = 2 \times 2$

The smallest prime number = 2

$$\text{HCF}(4, 2) = 2$$

Q12. If $\text{LCM}(x,18) = 36$ and $\text{HCF}(x,18)=2$, then find x ?

$\text{LCM} \times \text{HCF} = \text{product of numbers.}$

$$36 \times 2 = 18x$$

$$x = 36 \times 2 / 18 = 2 \times 2 = 4$$

Q13. The decimal expression of $27/ 2^3 5^4 3^2$ will terminate after how many decimal places?.

$$\begin{aligned} 27/ 2^3 5^4 3^2 &= 3^3/ 2^3 5^4 3^2 = 3^1 \times 2/ 2^4 5^4 \\ &= 6/10^4 = 0.0006 \end{aligned}$$

Hence, it will terminate after 4 decimal places.

Q14. The decimal expression of $6/1250$ will terminate after how many decimal places?.

$$\begin{aligned}6/1250 &= 2 \times 3 / 2 \times 5^4 = 2^4 \times 3 / 2^4 \times 5^4 \\ &= 16 \times 3 / 10^4 = 48 / 10000 = 0.0048\end{aligned}$$

Hence, it will terminate after 4 decimal places.

Q15. Find the HCF of 612 and 1314 using prime factorisation.

$$612 = 2 \times 2 \times 3 \times 3 \times 17 = 2^2 \times 3^2 \times 17;$$

$$1314 = 2 \times 3 \times 3 \times 73 = 2 \times 3^2 \times 73$$

$$\begin{aligned}\text{HCF}(612, 1314) &= 2 \times 3^2 \\ &= 18\end{aligned}$$

Q16. PROVE THAT $3-2\sqrt{2}$ IS IRRATIONAL, GIVEN THAT $\sqrt{2}$ IS IRRATIONAL

PROOF

1. Let us assume that $3-2\sqrt{2}$ is rational
2. Hence $3-2\sqrt{2} = a/b$, where a & b ($b \neq 0$) are co-prime numbers

$$2\sqrt{2} = 3 - a/b$$

$$\sqrt{2} = (3b-a)/2b$$

3. Since a and b are integers, we get $(3b-a)/2b$ is rational and so, $\sqrt{2}$ is rational.
4. This contradicts **the fact** that $\sqrt{2}$ is irrational
5. This contradiction has arisen because of our incorrect assumption that $3-2\sqrt{2}$ is rational
6. Hence $3-2\sqrt{2}$ is irrational

Q17. Explain why $3 \times 5 \times 7 + 7$ is a composite number.

$3 \times 5 \times 7 + 7 = 7(3 \times 5 \times 1 + 1) = 7 \times 16$, which has more than 2 factors. Hence, $3 \times 5 \times 7 + 7$ is a composite number.

Q18. Find the largest number which divides 77 and 85 leaving remainder 7 and 5 respectively.

The required largest number is the HCF of $(77-7)$ and $(85-5)$

$$70 = 2 \times 5 \times 7 ; 80 = 2 \times 2 \times 2 \times 2 \times 5$$

$$\text{HCF}(70, 80) = 2 \times 5 = 10$$

Q19. Find the largest number which divides 285 and 1249 leaving remainder 9 and 7 respectively.

The required largest number is the HCF of (285-7) and (1249-7)

$$276 = 2 \times 2 \times 3 \times 23 ; 1242 = 2 \times 3 \times 3 \times 3 \times 23$$

$$\text{HCF}(276, 1242) = 2 \times 3 \times 23 = 138$$

Q20. Find the largest positive integer that will divide 398, 436, 542 leaving remainders 7, 11 and 15 respectively

$$391 = 17 \times 23 ; 425 = 5 \times 5 \times 17 ; 527 = 17 \times 31$$

$$\text{HCF}(391, 425, 527) = 17$$

Q21. Find the largest number which divides 615 and 963 leaving remainder 6 in each case.

The required largest number is the HCF of (615-6) and (963-6)

$$609 = 3 \times 7 \times 29 ; 957 = 3 \times 11 \times 29$$

$$\text{HCF}(609, 957) = 3 \times 29 = 87$$

Q22. If $a = 2^3 \times 3$, $b = 2 \times 3$, $c = 3^n \times 5$ and $\text{LCM}(a, b, c) = 2^3 \times 3^2 \times 5$, then find n

$\text{LCM}(a, b, c) =$ greatest power

$$\text{LCM}(a, b, c) = 2^3 \times 3^n \times 5 = 2^3 \times 3^2 \times 5$$

Therefore $n=2$

Q23. Find the smallest number by which $\sqrt{8}$ should be multiplied to get a rational number?

$8 = 2 \times 2 \times 2$; if we multiply 8 with 2, we will get 16, which is a perfect square

$$\sqrt{8} \times \sqrt{2} = \sqrt{16} = 4$$

Hence the smallest number is $\sqrt{2}$

Q24. If $504 = 2^m \times 3^n \times 7^p$, then find the value of $m-n+p$?

$$504 = 2^3 \times 3^2 \times 7^1 = 2^m \times 3^n \times 7^p$$

Therefore $m=3, n=2, p=1$; $m-n+p=3-2+1=2$

Q25. Write the smallest number which is divisible by both 306 and 657?

$$306 = 2 \times 3 \times 3 \times 17 ; 657 = 3 \times 3 \times 73$$

$$\text{LCM}(306, 657) = \text{Highest powers}$$

$$= 2 \times 3 \times 3 \times 17 \times 73 = 22338$$

Q26. If p and q are prime numbers, then find HCF of p^3q^2 and p^2q

HCF = SMALLEST COMMON POWER

$$\text{HCF}(p^3q^2, p^2q) = p^2q$$

Q27. Find the least number that is divisible by first five even numbers.

The first 5 even numbers are 2,4,6,8,10

$2=2$; $4=2 \times 2$; $6=2 \times 3$; $8=2 \times 2 \times 2$; $10 = 2 \times 5$

$\text{LCM}(2,4,6,8,10) = 2 \times 2 \times 2 \times 3 \times 5 = 120$

Q28. The total number of factors of a prime number is

= 2(the number itself and one)

Q29. The sum of exponents of prime factors in the prime factorisation of 196 is

$196 = 2 \times 2 \times 7 \times 7 = 2^2 \times 7^2$

sum of exponents = $2+2=4$

Q30. The exponent of 2 in the prime factorisation of 144 is

$$144 = 2 \times 2 \times 2 \times 2 \times 3 \times 3 = 2^4 \times 3^2; \text{ Exponent of } 2 = 4$$

Q33. $(2 + \sqrt{5})/3$ isnumber (ans = irrational)

Q34. The decimal form of $129/2^2 5^7 7^5$

= non-terminating non-repeating, since 7^5 is there in the denominator

Q35. The product of a rational number and irrational number(irrational)

Q36. The sum of a rational number and irrational number(irrational)

Q37. The product of two different irrational numbers is always

- (a) Rational (b) irrational (c) both of the above
(d) none of the above

Reason : $\sqrt{2} \times \sqrt{8} = \sqrt{16} = 4$ (rational)

$$\sqrt{2} \times \sqrt{3} = \sqrt{6} \text{ (irrational)}$$

Q38. If $b=3$, then any integer can be expressed as

- (a) $3q, 3q+1, 3q+2$; (b) $3q$; © none of the above, (d) $3q+1$

Q39. The product of three consecutive positive is divisible by (a) 4 (b) 6 © no common factor(d) only 1

$$1 \times 2 \times 3 = 6/6 = 1$$

$$2 \times 3 \times 4 = 24/6 = 4$$

$$3 \times 4 \times 5 = 60/6 = 10$$

$$4 \times 5 \times 6 = 120/6 = 20$$

Q40. The set $A = 0, 1, 2, 3, 4, 5, \dots$ Represents the set of WHOLE numbers

Q41. For some integer p , every even integer is of the form (a) $2p+1$ (b) $2p$ © $p+1$ (d) p

Q42. For some integer p , every odd integer is of the form (a) $2p+1$ (b) $2p$ © $p+1$ (d) p

Q43. The product of two consecutive natural numbers is always (a) Prime number (b) even number (c) odd number (d) even or odd

$$1 \times 2 = 2; 2 \times 3 = 6; 3 \times 4 = 12; 4 \times 5 = 20; 5 \times 6 = 30$$